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INFLUENCE OF A MAGNETIC FIELD ON QUARTZ CRYSTAL RESONATORS

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ABSTRACT

The magnetic sensitivity of quartz crystal resonators is a consequence of the ferromagnetic properties of the metal used as support for the vibrating plate. Various magneto-mechanic interactions can contribute to the overall sensitivity, the most important of which is shown to be the change in Young's modulus of the spring material submitted to a magnetic field, which in turn modifies the stress in the quartz plate and then induces a change in the crystal resonant frequency. The experimental setup and procedure are described and a large number of experimental results obtained with resonators of different technologies are presented and discussed. A comparison between the magnetic behavior of identical resonators mounted with different materials definitely proves the responsibility of the supports in the magnetic sensitivity of resonators and gives interesting information on its reduction.

I. INTRODUCTION

As the oscillator performance increases, new applications such as precision orbit determination need more and more accurate devices. In fact, the measurement accuracy of the positioning systems using the Doppler effect strongly depends on the frequency stability of the master oscillator. As an example, the DORIS mission, whose goal is to locate a satellite with a precision of 10 cm, requires a frequency stability of the on-board oscillator of 5.10^{-13} [1]. It is well known that most of the frequency instabilities are due to temperature variation, acceleration or ionizing radiation. Many efforts have been made to improve oscillator performance either by using selected components insensitive to the environmental variations or by shielding the oscillator against these variations. For the past few years, attention has been focused on magnetic field effects, because it was observed that starting or stopping on-board magnetic stabilizing equipment may lead to a slight frequency shift in a nearby oscillator. The order of magnitude of this oscillator magnetic sensitivity, which is about $10^{-11}/\text{G}$ does not permit the stability specification to be fulfilled. A number of studies have been undertaken to identify the origin of the oscillator magnetic sensitivity [2]-[4]. The studies have shown that almost all components of the oscillator circuitry may have a more or less important effect [5]-[7]. Of course, among the studied components, the quartz resonator has been given special attention because of its major role in the oscillator. From the experimental point of view, the magnetic sensitivity is easy to see on the oscillator as a whole but it is more difficult to measure the contribution of the individual components since they have to be kept in the magnetic field far from the other parts of the oscillator. To increase the signal to noise ratio, the magnetic field used in the experiment lies typically in the

range of ± 40 G (± 4 mT) which is larger than the actual value the oscillators typically experience which is in the range ± 10 G (± 1 mT).

II. EXPERIMENTAL SETUP AND PROCEDURE

A. Resonators

Most of the tested resonators are regular commercially available units in the range 5 to 10 MHz, fifth or third overtone, AT or SC cut operating in the low shear mode (C-mode). The internal assembly of one of these resonators is shown in Fig. 1, the quartz disc is held by two nickel springs soldered on two kovar supports. This latter material is used because it has the same thermal expansion coefficient as the insulating glass through which the supports pass. The electrical connection between quartz electrodes and springs is provided with a conducting silver-filled cement. The resonator is maintained under vacuum by a gold-plated copper cap cold-welded to a kovar base. In most cases, electrodes were made of a 700-Å gold layer deposited on a 20-Å chrome underlayer. In some samples, electrodes were also made of aluminum.

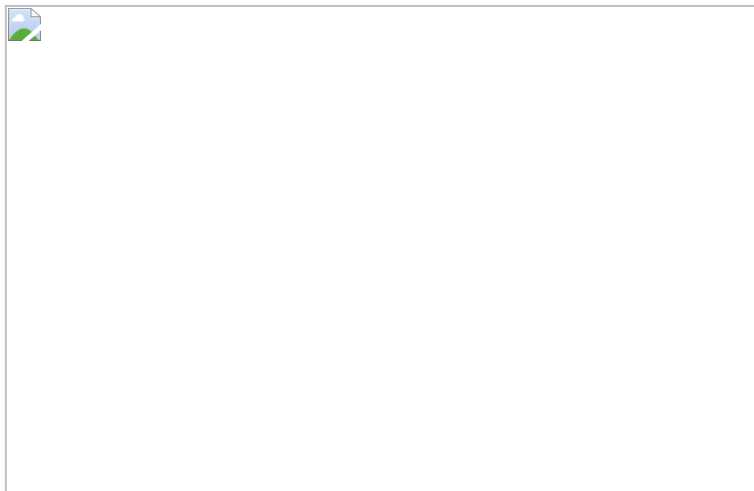


Figure 1. Internal assembly of a resonator.

B. Magnetic Field Production and Measurement

Preliminary experiments [8] have shown that the magnetic sensitivity of oscillators and resonators strongly depends on the orientation of the magnetic field. Furthermore, it is highly desirable that the device under test keeps the same position in all experiments so as to avoid errors due to the earth's magnetic field or to gravitational effects when rotating the device rather than the magnetic field [9]. To this end, in all experiments, the resonator was held in a fixed position, the symmetry axis being always vertical (see Fig. 2).

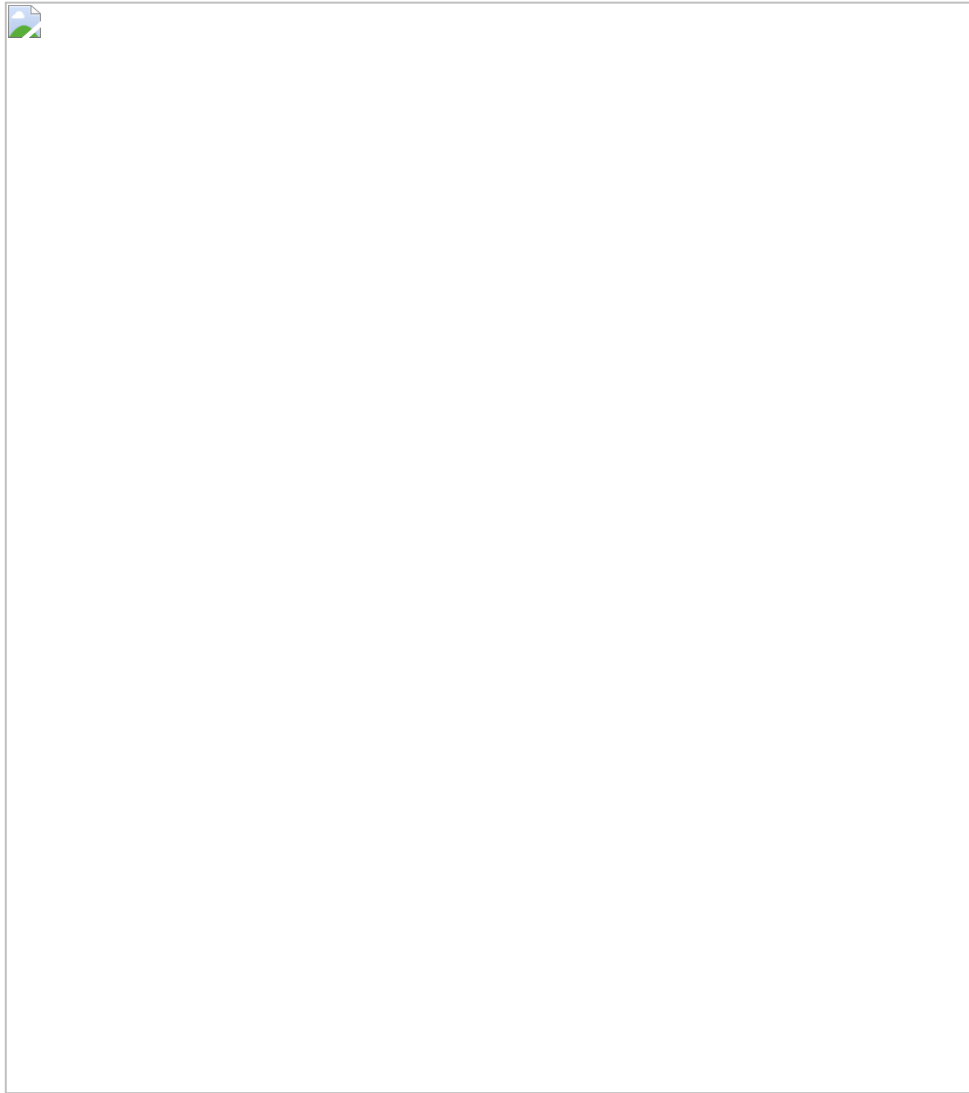


Figure 2. Experimental setup.

In order to give the magnetic field vector different orientations with respect to the resonator, the magnetic field is produced by using two pairs of Helmholtz coils. One of them is fixed to produce a vertical magnetic field along the symmetry axis of the resonator, the other pair can go around the symmetry axis thus enabling any radial orientation of the magnetic field in a plane normal to the symmetry axis (see Fig. 3). The origin for the radial orientation is arbitrarily set to zero when the magnetic field is normal to the plane containing the two supports. Measurement of the magnetic field nonuniformity shows that it is below the resolution of the gaussmeter in the relevant area i.e. less than 0.15 G in a volume $10 \times 10 \times 10 \text{ cm}^3$. The magnetic field gradient can thus be estimated to be less than 1.5 G/m (0.15 mT/m) for a nominal magnetic field of 20 G (2 mT). In all the experiments, the most important source of perturbation comes from the temperature effects. To reduce these effects, the resonator under test is kept at its turnover point, in an oven placed in a Dewar flask.



Figure 3. Possible magnetic field orientations. (b) Main direction definitions.

To assess the temperature stability of the measurement setup, one of the resonators to be tested were operated in the B-mode, so that it acted as a temperature sensor with sensitivity $-33 \text{ ppm}/^{\circ}\text{C}$. Several measurements have shown that, when the temperature equilibrium is reached, the temperature stability of the oven is better than 10^{-4}°C over the experimental duration; that is, about 100 s. If it is assumed that the temperature is not exactly set at the turnover point when operating in the C-mode, resulting in a residual temperature sensitivity about $2 \cdot 10^{-7}/^{\circ}\text{C}$, the overall relative frequency fluctuation induced by the temperature variation remains within $2 \cdot 10^{-11}$. This is one or two orders of magnitude below the magnetic effect.

The oscillator circuit is kept in a separate oven far from the magnetic field so as to avoid unwanted magnetic effects on the other parts of the oscillator. Nevertheless, temperature effects and other environmental perturbations can still affect the measurement through the rigid coaxial cable needed to connect the resonator to the oscillator circuit. In order to improve the signal to noise ratio, the magnetic field is given a low frequency sinusoidal modulation enabling the use of the signal processing method described below. The driving current in the coils coming from a low frequency generator through a power amplifier provided a magnetic field in the range $\pm 40 \text{ G}$ ($\pm 4 \text{ mT}$). It is measured by means of a gaussmeter using two Hall effect probes located near the resonator, one probe for axial field measurement and the other one for radial field measurement.

C. Magnetic Sensitivity Measurement and Data Processing

In most cases, the overall frequency shift observed lies in the range 10^{-9} when the resonator is submitted to the magnetic field previously described. The measurement of such small variations is performed by using the popular method represented in Fig. 4.

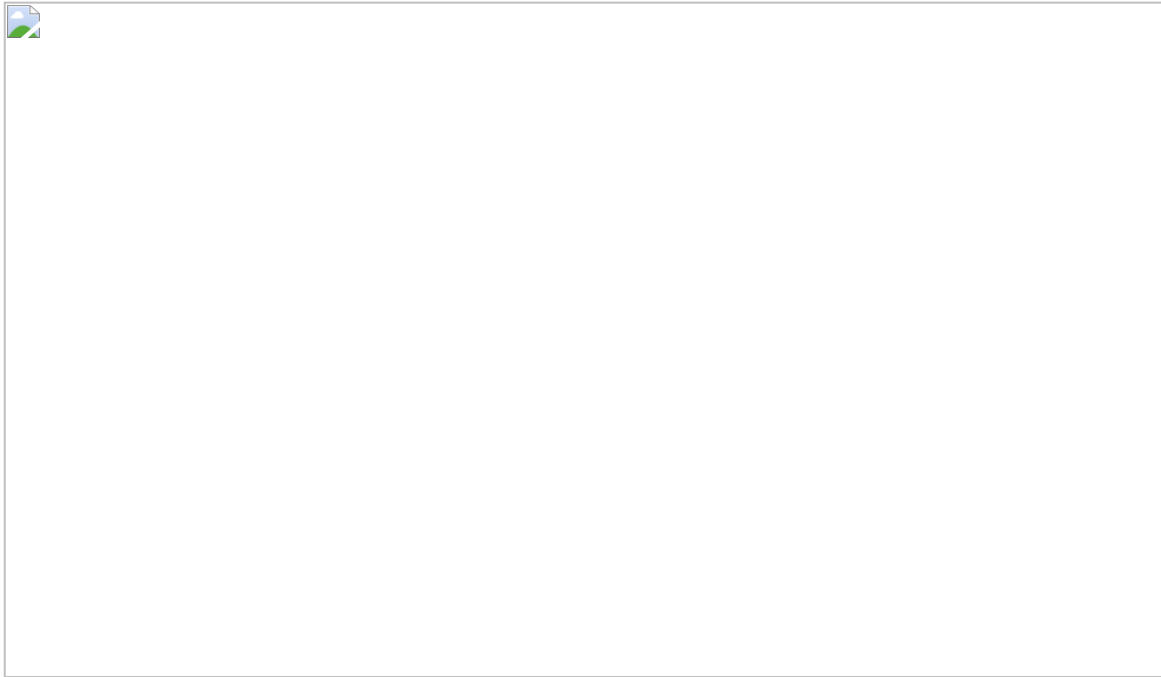


Figure 4. Measurement setup.

The frequency of the oscillator under test is compared with a reference oscillator by using a balanced mixer, a low noise amplifier and a low pass filter. The beat frequency reproducing the oscillator frequency variation is usually in the range from a few tens to a few hundred hertz and can thus be measured with an enhanced resolution by means of a frequency counter. This frequency variation as well as the magnetic field are simultaneously sampled and stored as a function of time in a microcomputer. The entire experiment is automated by using an IEEE-488 bus interface. The period of the low magnetic field excitation has been chosen to meet two opposing requirements: it has to be long enough to insure that no dynamic magnetic effects can occur and short enough to avoid long-term temperature drift, which could affect the accuracy of the data processing. Some preliminary experiments performed in various conditions have shown that an excitation period of 100 s and a sampling time of 1 s constitute a satisfactory compromise. In the actual experimental setup, relative frequency variations of a few parts in 10^{12} can be seen with a reasonable reproducibility.

Because of the periodic character of the magnetic field excitation and the resonator frequency response, it is possible to average the data over a number of periods (usually several tens). In fact, it is well known that in such a case, the signal-to-noise ratio increases as the square root of the cycle number. In addition, the low-frequency variations due to the temperature drift can be partially removed by performing a first-order regression on each period of the excitation signal. Fig. 5 demonstrates the effect of this data processing. Fig. 5(a) and (b) shows the frequency versus time and the frequency versus magnetic field raw data, and Fig. 5(c) shows the result obtained after the averaging and regression processes have been performed. As shown in Fig. 5(c), the data processing also corrects for the sign reversal due to a reference frequency higher than the measured frequency (see Fig. 4).

In most cases, the magnetic sensitivity is measured in the three main directions shown in Fig. 3(b). Fig. 6 shows a typical example of the results thus obtained. It should be noted that the records are quite reproducible, as demonstrated by Figs. 6(c) and 7, which show two different records performed on the same resonator with the same magnetic field orientation. In these figures, the origin of the vertical axis, arbitrarily chosen, has no particular significance.



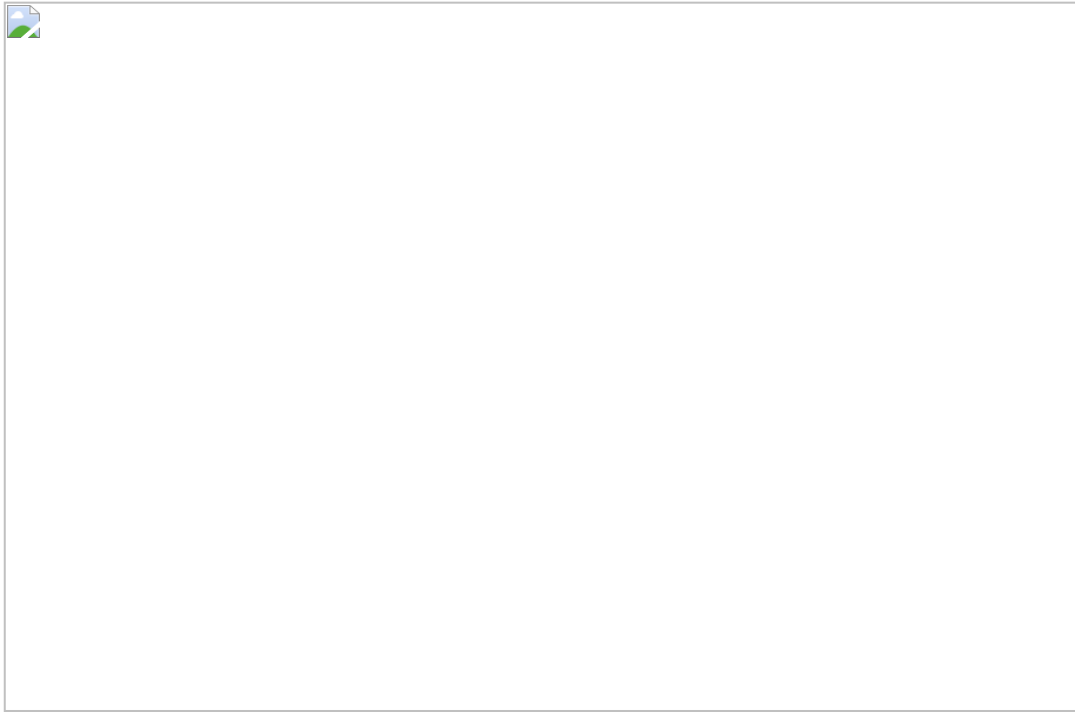
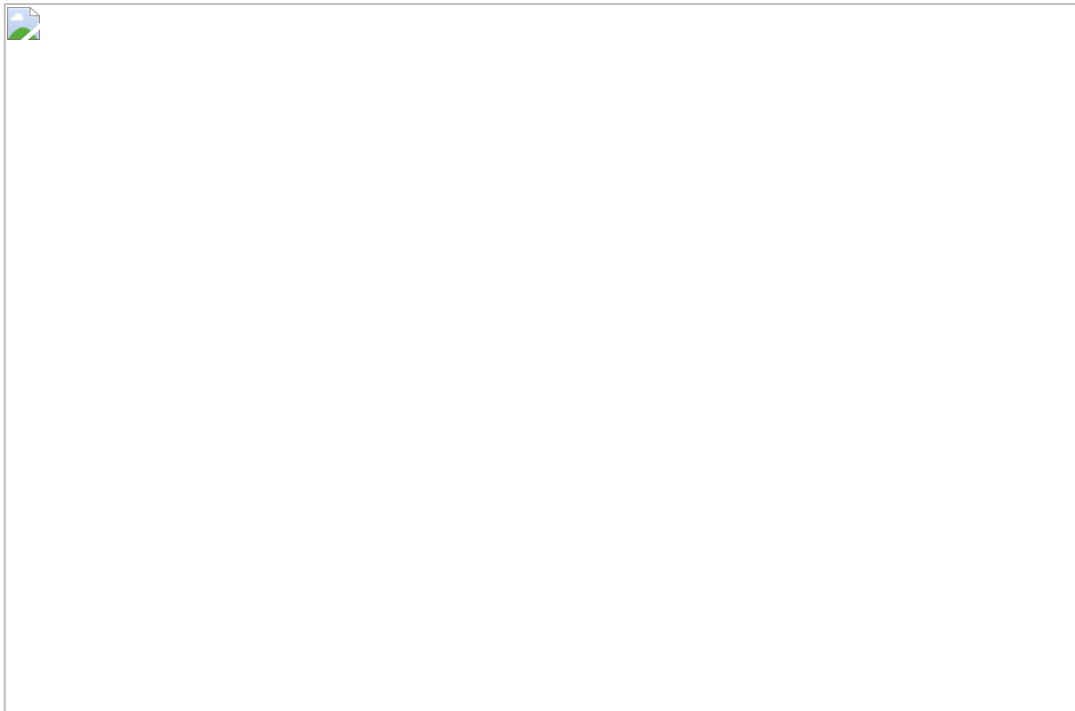


Figure 5. (a) Raw data frequency shift versus time. (b) Raw data frequency shift versus magnetic field. (c) Averaged result with drift and sign corrections.



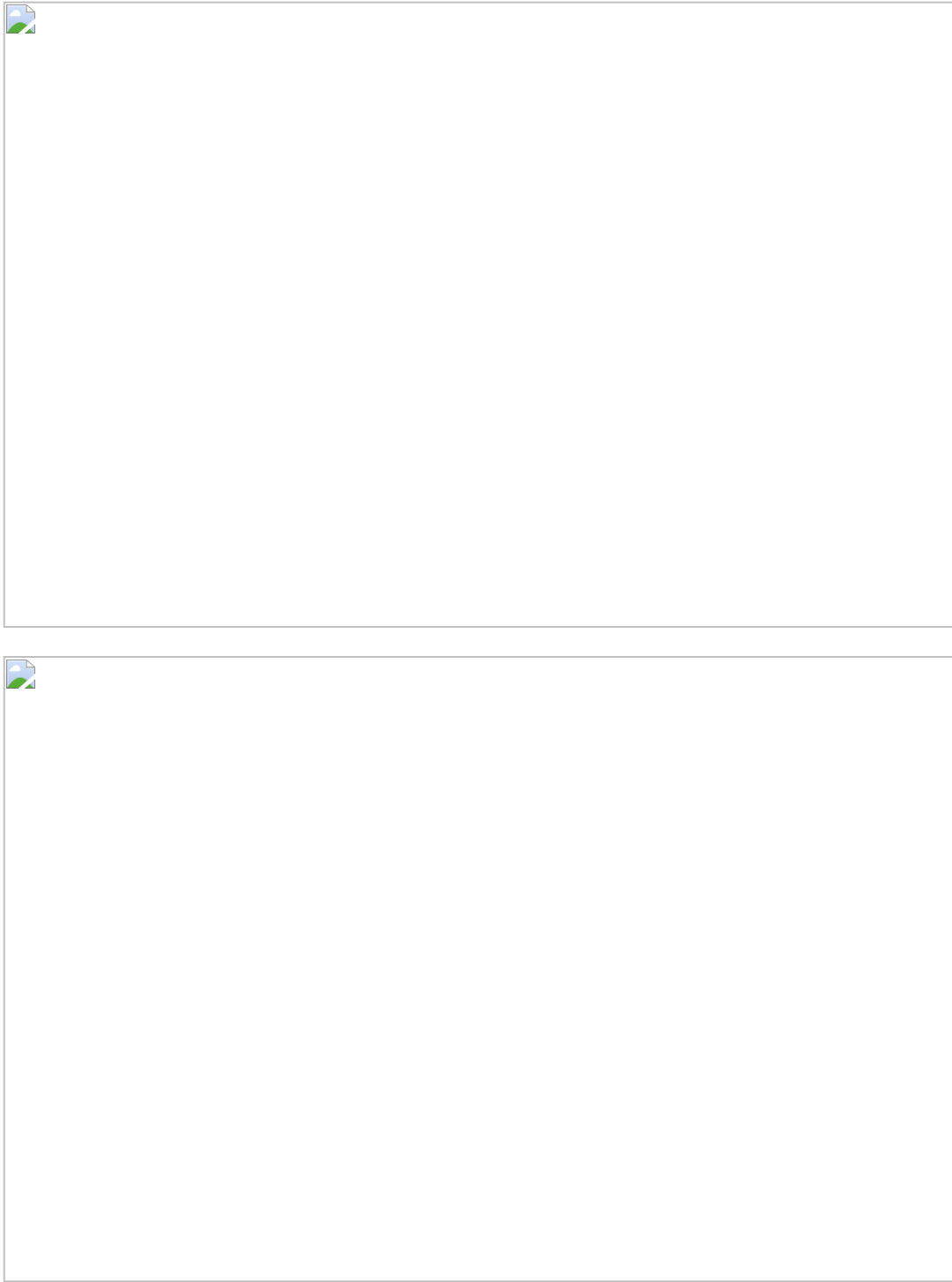


Figure 6. Magnetic sensitivity of a regular resonator with magnetic field: (a) normal to the support plane, (b) in the support plane, and (c) along the symmetry axis.

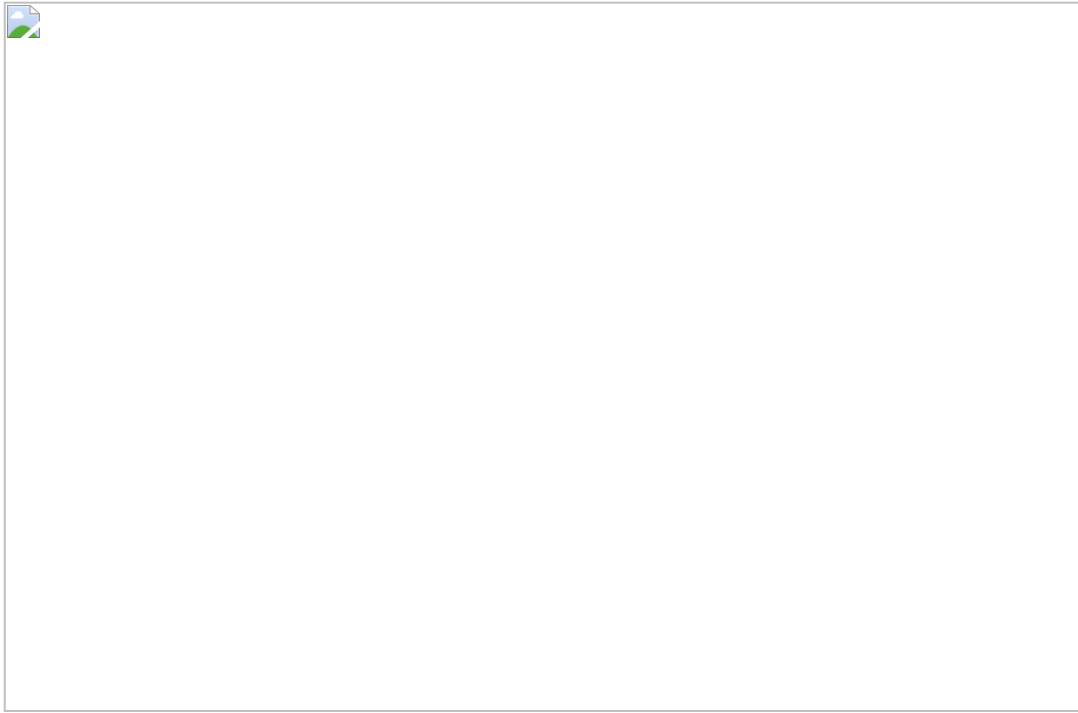


Figure 7. Another record performed on the same resonator as in Fig. 6(c) demonstrates the reproducibility of the phenomenon.

III. INFLUENCE OF SOME EXPERIMENTAL CONDITIONS

A. Orientation

On some samples, the magnetic sensitivity curve is not symmetrical with respect to the vertical axis as it should be in regard to the geometrical symmetry of the resonator arrangement. Sometimes, this effect is due to a misalignement of the sample with respect to the magnetic field as demonstrated in Fig. 8, nevertheless, in many cases the asymmetry of the curve does not depend on the orientation of the resonator and could reveal in fact an asymmetry in the internal assembly of the device; this point will be further discussed later.

Fig. 9 shows the records obtained when the magnetic field is rotated around the symmetry axis of the resonator. In this case, the maximal sensitivity is observed when the magnetic field lies in the support plane (90° or 270°).



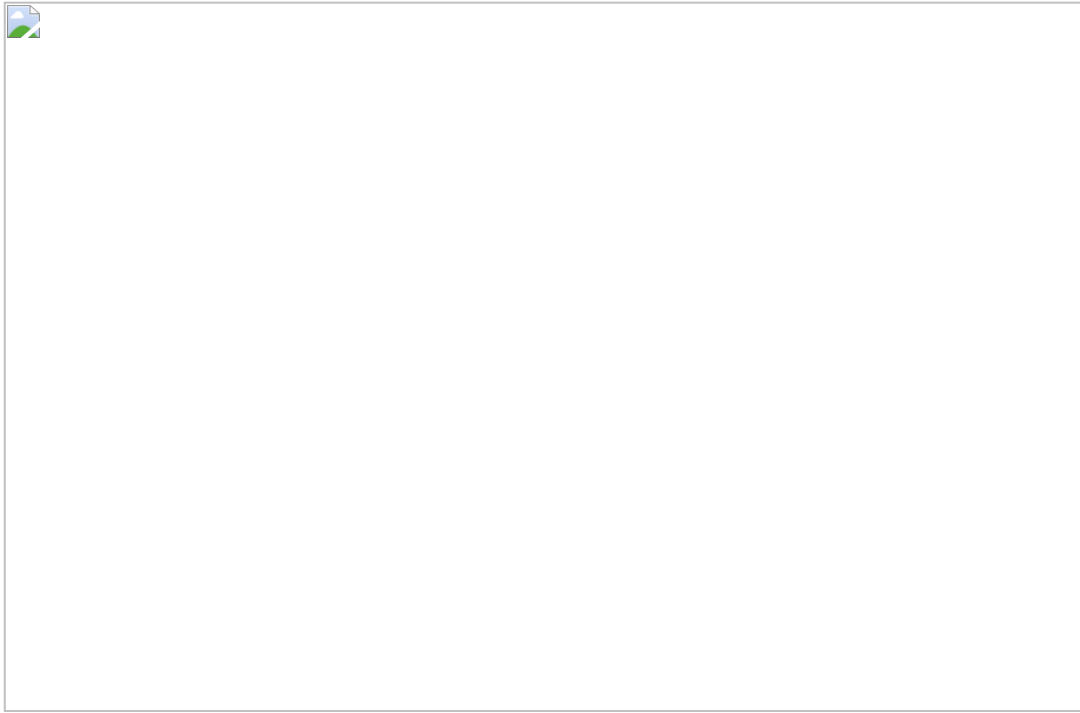


Figure 8. Effect of a slight rotation around the symmetry axis of the resonator.
(a) Tangent field -5° . (b) Tangent field $+5^\circ$. (c) Tangent field $+0^\circ$.

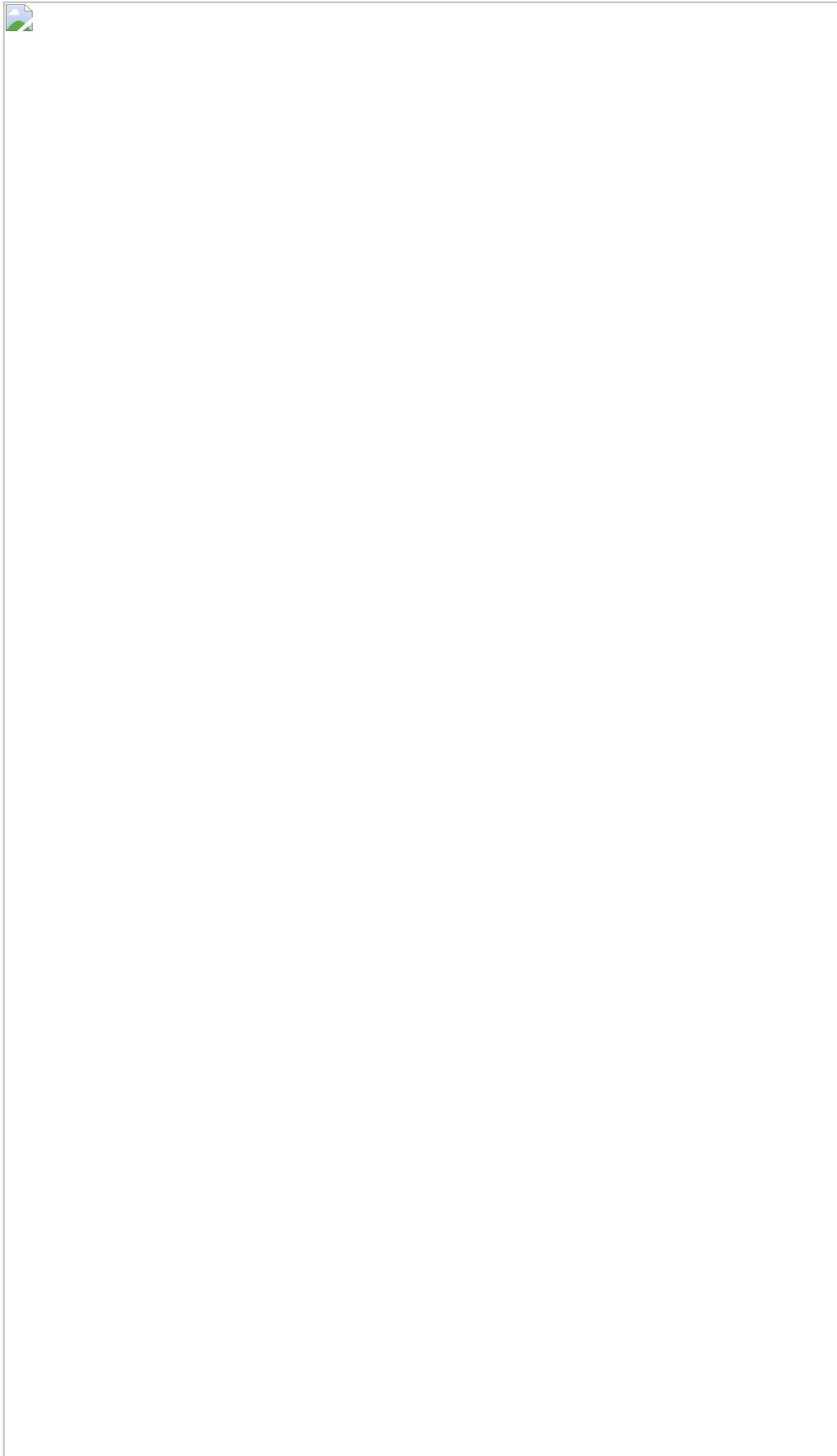


Figure 9. Magnetic sensitivity obtained when rotating the magnetic field around the symmetry axis of the resonator.

B. Magnetic Field Strength

The amplitude of the magnetic field used in the experiments has been chosen so as to obtain a sufficient signal-to-noise ratio. Nevertheless, the shape and the amplitude of the magnetic sensitivity "*signature*" of a resonator strongly depend on the strength of the applied magnetic field, as seen in Fig. 10; it represents the records obtained on the same resonator with smaller and smaller magnetic field amplitude. Note that the low level behavior noticeably differs from the higher level behavior, so that it is dangerous to extrapolate the low level sensitivity from a high level measurement. As a consequence, the magnetic sensitivity of a resonator, or any other component as well, should never be given without specifying the magnetic field amplitude used for the measurement. Recommendations for the operating procedure to be used for magnetic sensitivity measurement are currently being published [\[10\]](#).

C. Magnetic Field Offset

Fig. 11(a) shows the magnetic sensitivity of a QHS 10-MHz SC-cut resonator while fig. 11(b) shows the results obtained on the same resonator when giving the magnetic field a dc offset of, respectively, -10, 0 and +10 G superimposed on the main slowly varying magnetic field. As expected, the magnetic signature strongly depends on the magnetic polarization of the material. In addition, when comparing Fig. 11(a) and (b) it can be observed that the shifted magnetic signature in Fig. 11(b) approximately follows the corresponding part of the main cycle in Fig. 11(a).



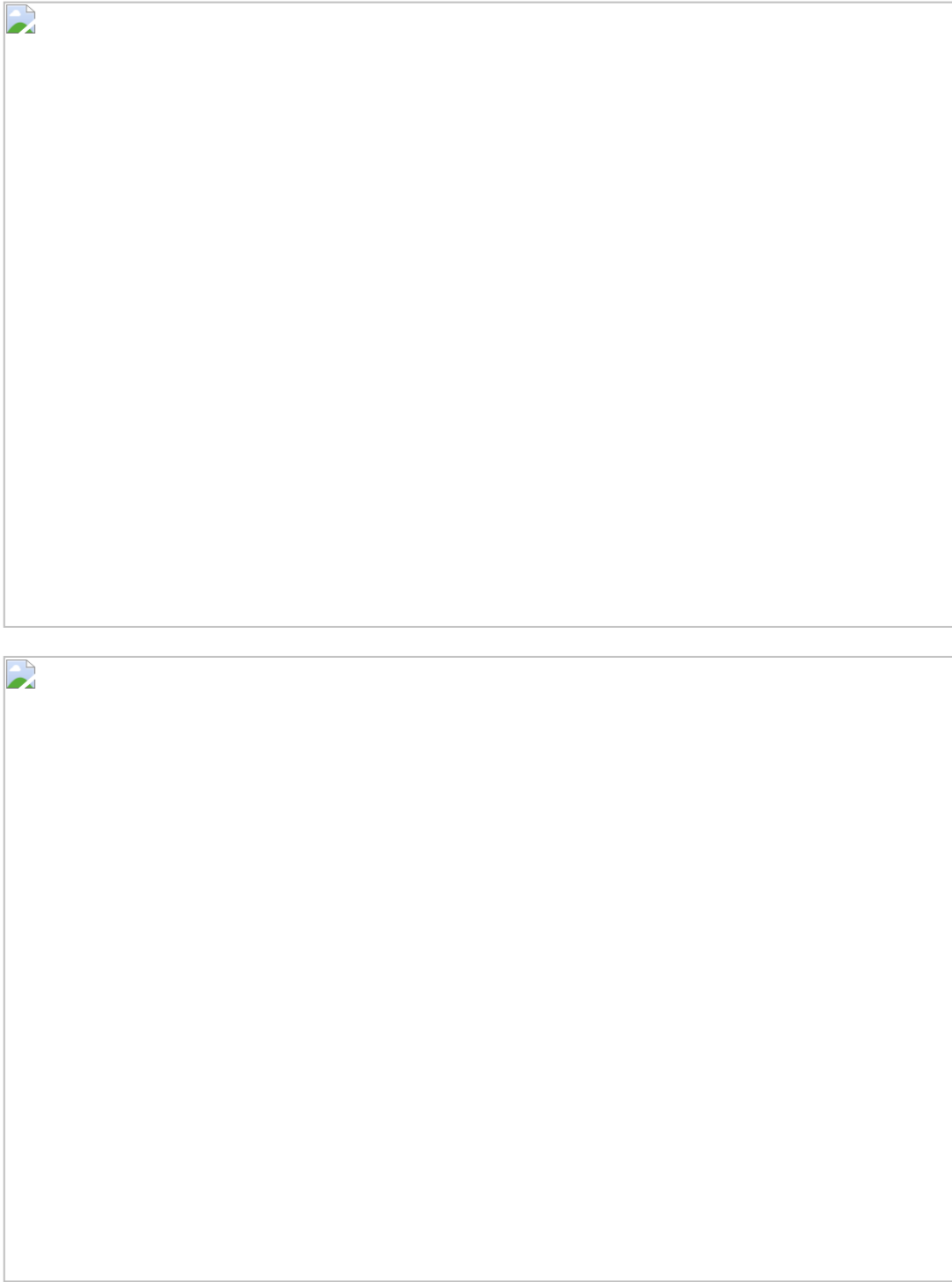


Figure 10. Magnetic sensitivity curves obtained with smaller and smaller magnetic field amplitude. (a) Amplitude ± 40 G (± 4 mT). (b) Amplitude ± 20 G (± 2 mT). (c) Amplitude ± 10 G (± 1 mT).

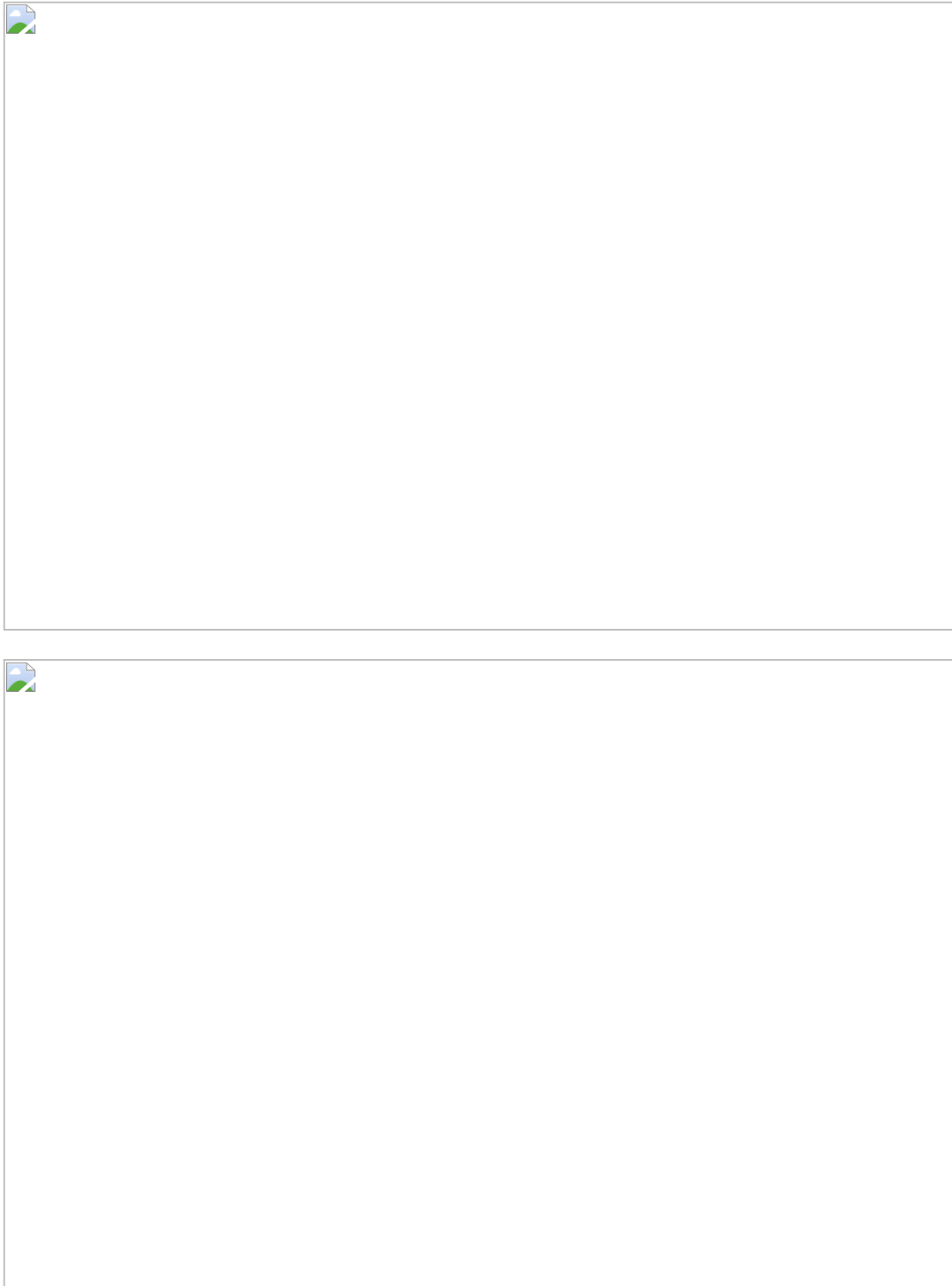


Figure 11. Influence of a dc magnetic field offset on the magnetic sensitivity of a QHS 10-MHz SC-cut resonator. (a) Amplitude ± 20 G (± 2 mT) without offset. (b) Amplitude ± 10 G (± 1 mT) with offset -10 G, 0, +10 G.

D. Temperature

Magnetic sensitivity of a resonator measured at various temperatures within the range 60-80°C (Fig. 12) shows that the overall amplitude of the curve slightly decreases when the temperature increases (about 8% for 20°C). The shape of the signature remains practically unchanged. Due to the weakness of this effect it has not been further investigated.



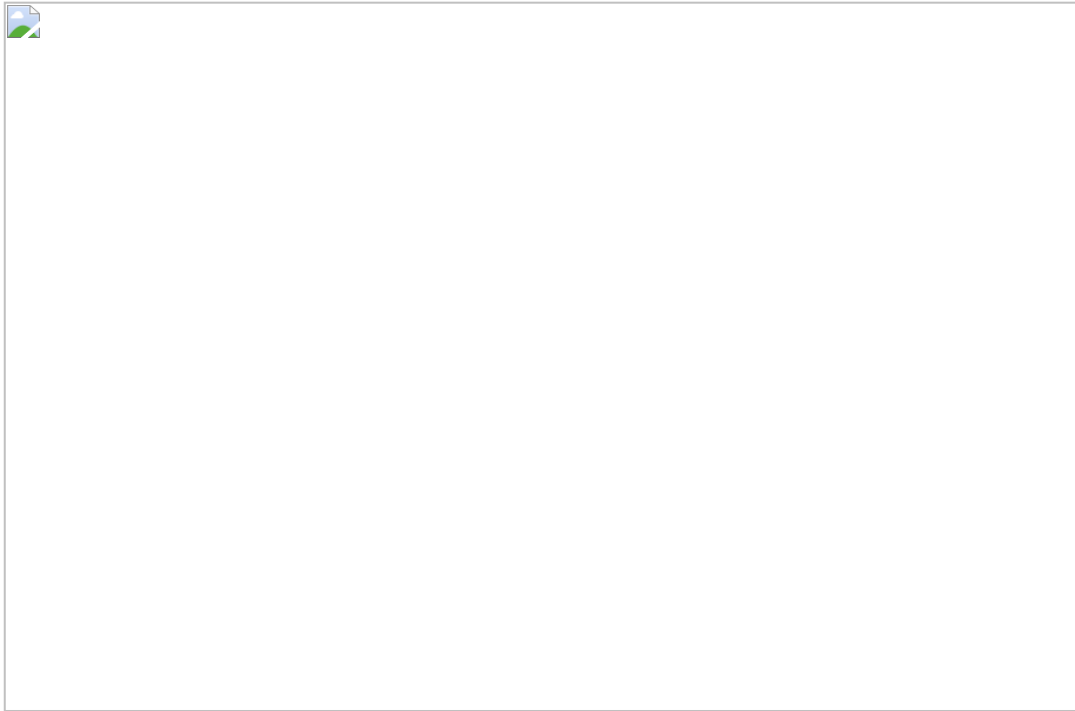


Figure 12. Influence of the temperature on the resonator magnetic sensitivity. (a) Temperature 59°C. (b) Temperature 69°C. (c) Temperature 81°C.

IV. INFLUENCE OF THE RESONATOR TECHNOLOGY

More than 20 resonators of various cut, frequency, support material and/or enclosure have been measured in the three main directions [Fig. 3(b)]. Only a selected number of results will be reported here.

A. QHS Technology

The name used by the manufacturer (THOMSON-CEPE, F-95105 Argenteuil Cedex) is used to designate the regular resonators. The results shown in Fig. 13 have been obtained with 10-MHz third-overtone SC-cut resonator using nickel springs in T2111 box enclosure (MIL HC40/U). Only the results obtained in the most sensitive direction, along the symmetry axis, are shown.

Figs. 13(a) and (b) show the results obtained with two QHS resonators from the same batch, and Fig. 13(c) is obtained with another resonator of same technology from another batch. The most surprising fact when looking at these results is the great variety of "*magnetic signature*," while the overall amplitude keeps approximately the same order of magnitude.



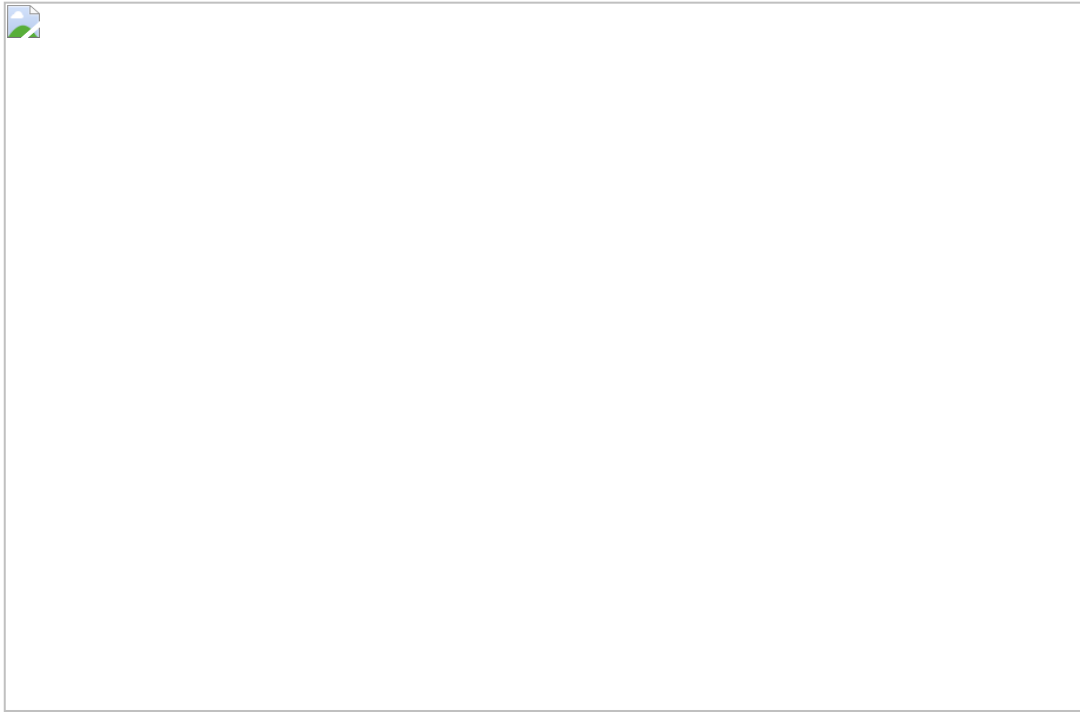
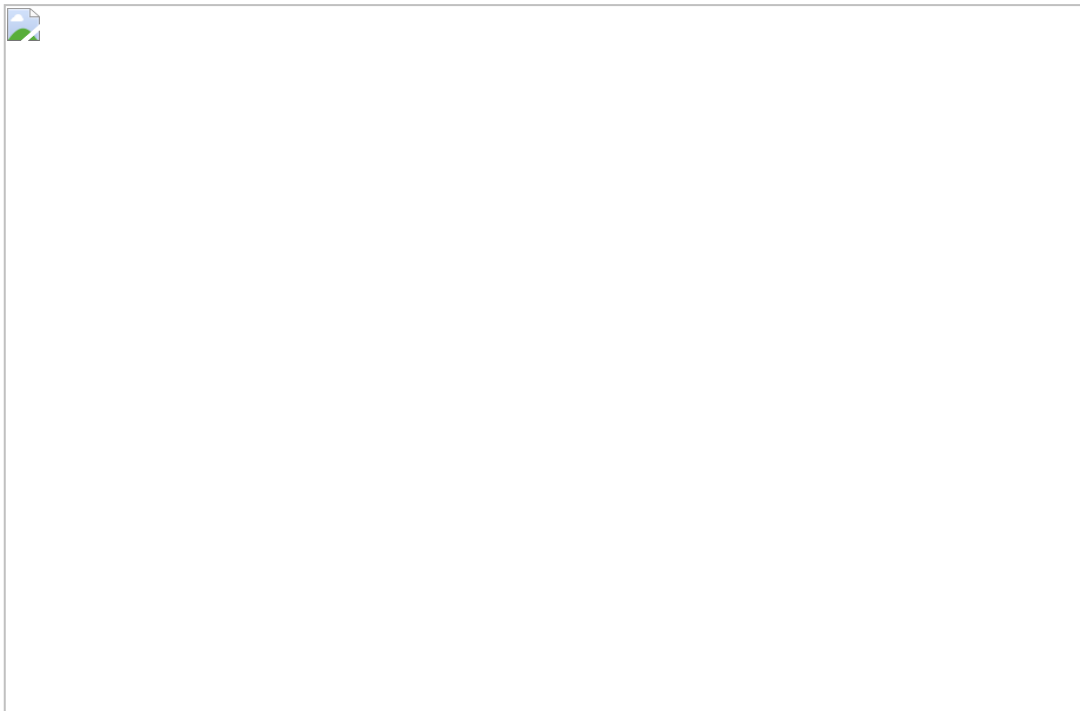


Figure 13. Magnetic sensitivity of QHS 10-MHz SC-cut resonators. (a) Batch 9125 sample 1/015/09. (b) Batch 9125 sample 1/015/10. (c) Batch 9122 sample 1/792/15.

B. QAS Technology



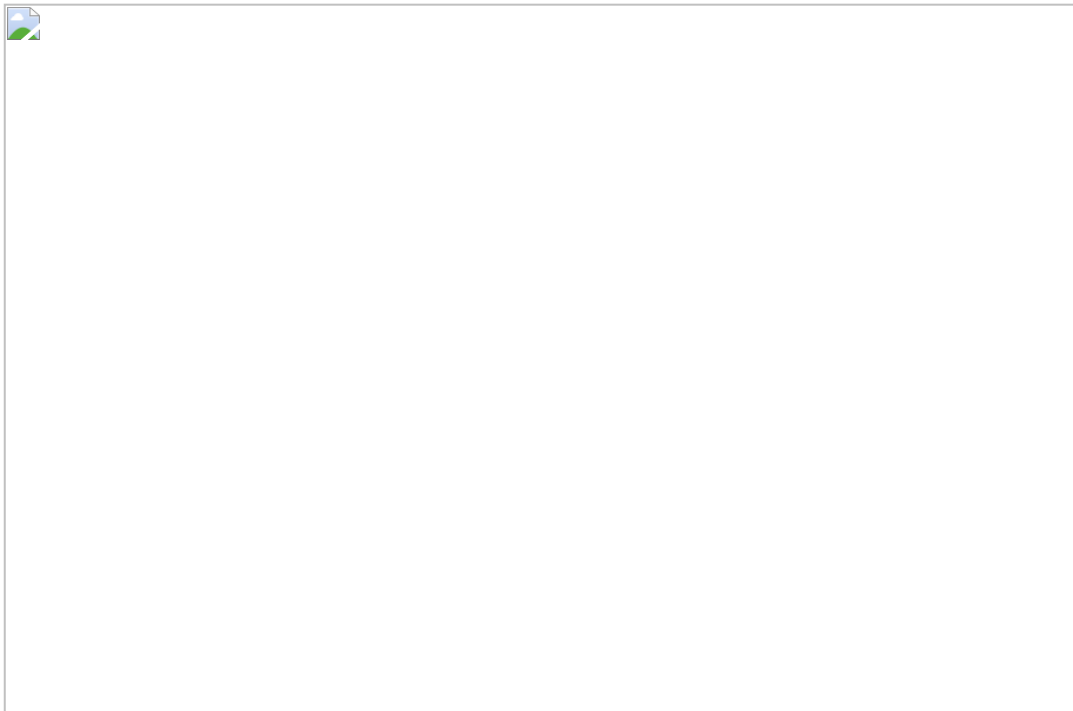
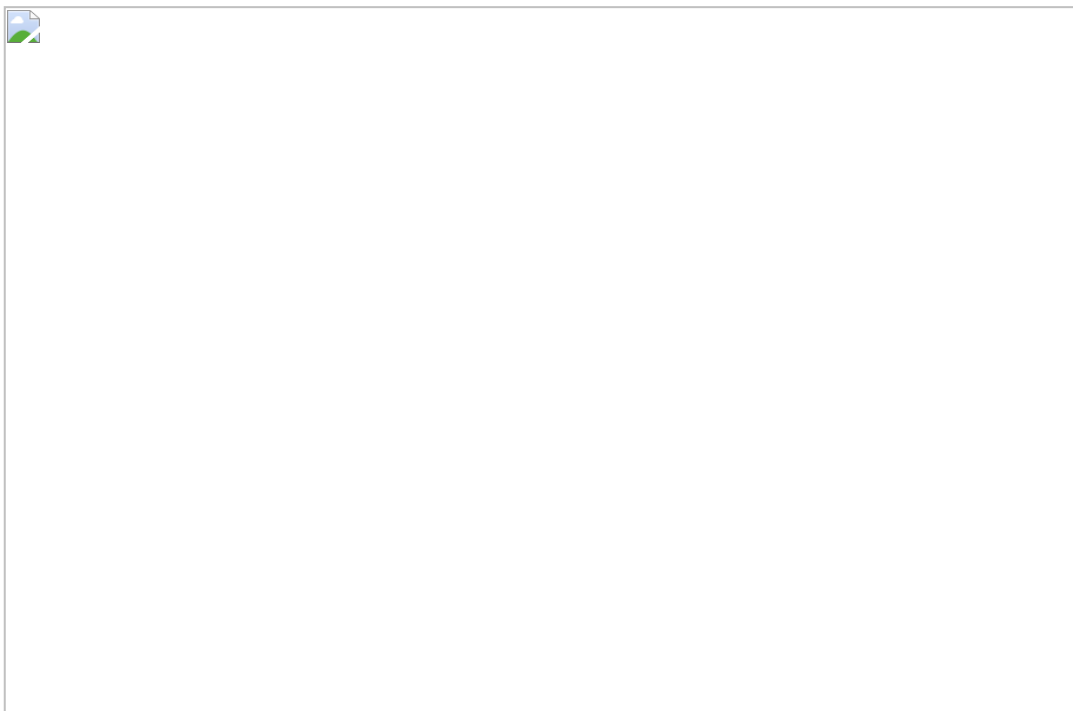


Figure 14. Magnetic sensitivity of QAS 10-MHz SC-cut resonators. (a) Batch 9137 sample 1/096/04. (b) Batch 9137 sample 1/096/12.

These resonators differ from the previous resonators by the fact the vibrating part of the crystal plate is sustained by small quartz bridges connected to a concentric quartz ring supported by nickel springs. This arrangement intends to isolate the vibrating part of the plate from the support stresses. Figs. 14(a) and (b) are obtained with two QAS from the same batch. Their magnetic signatures are fairly similar but much larger than those of QHS (the scale in Fig. 14 is four times larger than the scale of Fig. 13).



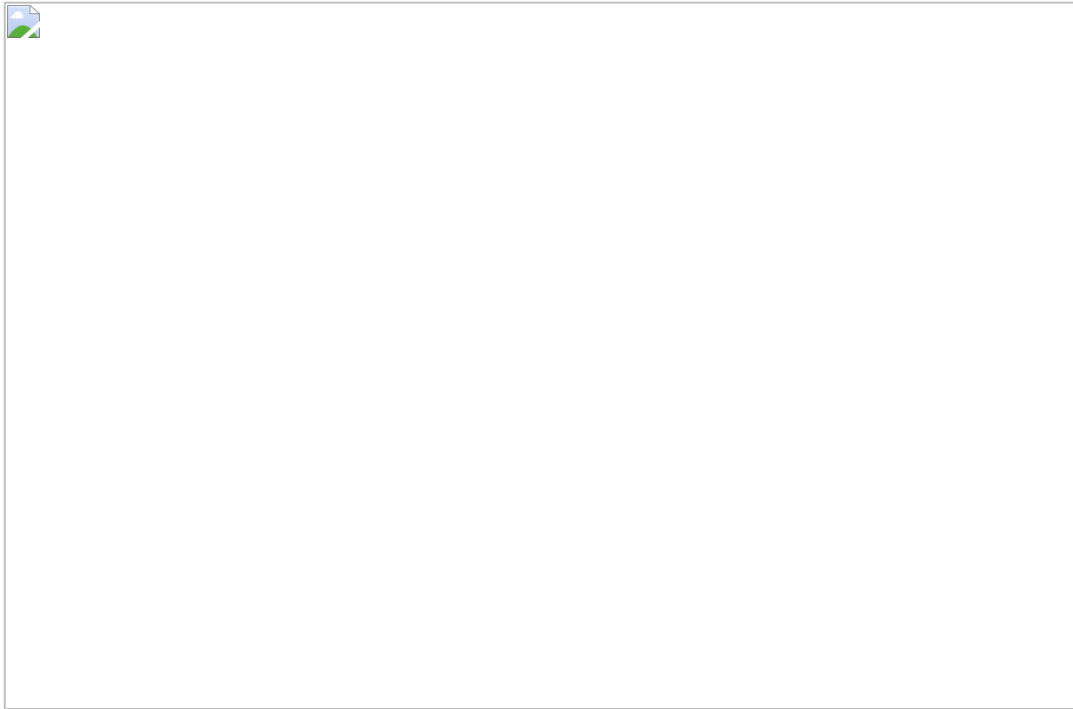


Figure 15. Magnetic sensitivity of QAS 10-MHz SC-cut resonators: (a) without intermediate plate and (b) with intermediate plate.

Another experiment has been performed to compare the results obtained with two QAS resonators. One of resonators [Fig. 15(a)] is a regular one, the other resonator is mounted on an intermediate plate [Fig. 15(b)]. The barometric sensitivity of the first resonator has been measured to be 25 times larger than the second, while its overall magnetic sensitivity is six times larger. It will be shown in the next section that the magnetic sensitivity of the resonator comes from the ferromagnetic properties of the spring material. The most probable magneto-elastic mechanisms involved in the resonator sensitivity are even functions in the applied magnetic field and the frequency shift versus magnetic field curves would present the same symmetry and should be also even functions in the magnetic field. This is almost true in a number of figures presented in this paper, but this is not always the case [see, for example, Figs. 13(b) and 15(a)]. It is highly probable that the asymmetry of the magnetic sensitivity curves reveals in fact an asymmetry in the mechanical mounting of the quartz plate. As a consequence, the stress induced in the plate by the magneto-elastic effects in the springs is no longer symmetrical with respect to the plate axis, and the resulting frequency shift loses the initial symmetry of the phenomenon. Hence the high barometric sensitivity of the resonator used for Fig. 15(a) could be explained by a mounting asymmetry revealed by the strong asymmetry of the magnetic sensitivity curve. Indeed, it is well known that any asymmetry in the mechanical assembly of a resonator drastically increases its sensitivity to environmental perturbations (acceleration, pressure, etc.) [\[11\]](#).

C. BVA Resonators

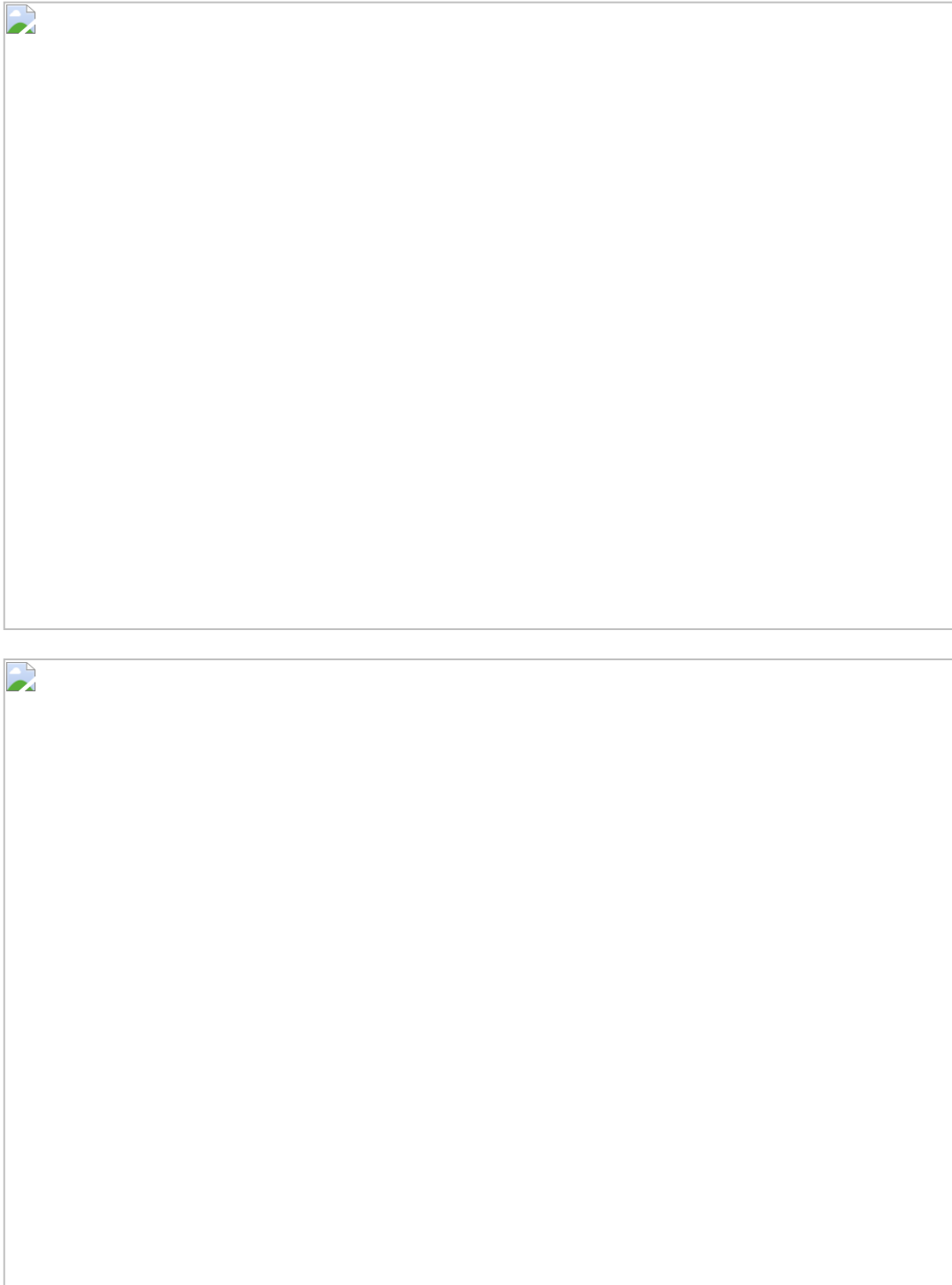


Figure 16. Magnetic sensitivity of two BVA 10-MHz SC-cut resonators. (a) Sample 17/02. (b) Sample 27/07.

As in the QAS resonator, the vibrating part of the crystal plate of a BVA resonator is connected to a concentric ring by quartz bridges. In addition, the ring is gripped between two adjacent quartz plates which support the electrodes which are then not directly deposited on the active part of the vibrating plate [12]. This arrangement has proved to be much less sensitive to environmental conditions than the regular resonators. Fig. 16 shows that this is also true for the magnetic sensitivity.

D. Spring Material

The magnetic sensitivity of quartz resonators has been observed for a long time and several explanations on its physical origin have been given [2], [3], [13]. A few years ago we demonstrated that this sensitivity comes from the ferromagnetic properties of the plate supports [6]. This point will be further developed in the next section.

Since then, many efforts have been made to reduce the magnetic sensitivity of the resonator, including testing materials different from the nickel usually used. A set of five resonators has been investigated. All of the resonators are identical, except the mounting springs are made of different materials. The resonators are all 6.144-MHz AT-cut QHS units. Because of the particular frequency of these resonators the experimental conditions have been slightly modified, the curves obtained, shown in Fig. 17, are then a bit more noisy, nevertheless they remain worth reading. They are presented from the greatest to the least magnetic sensitivity. The kovar appears to be much more sensitive than the nickel while stainless steel is noticeably less sensitive. It is not surprising that the resonator made with copper-alloy springs does not exhibit any perceptible magnetic sensitivity. This last experiment definitely proves the responsibility of the magnetic properties of the springs for the magnetic sensitivity of resonators. Of course, a reduced magnetic sensitivity is not the only goal to reach, the resonators still have to keep their performance in terms of mechanical behavior, accelerometric and barometric sensitivity, aging, etc [\[14\]](#).

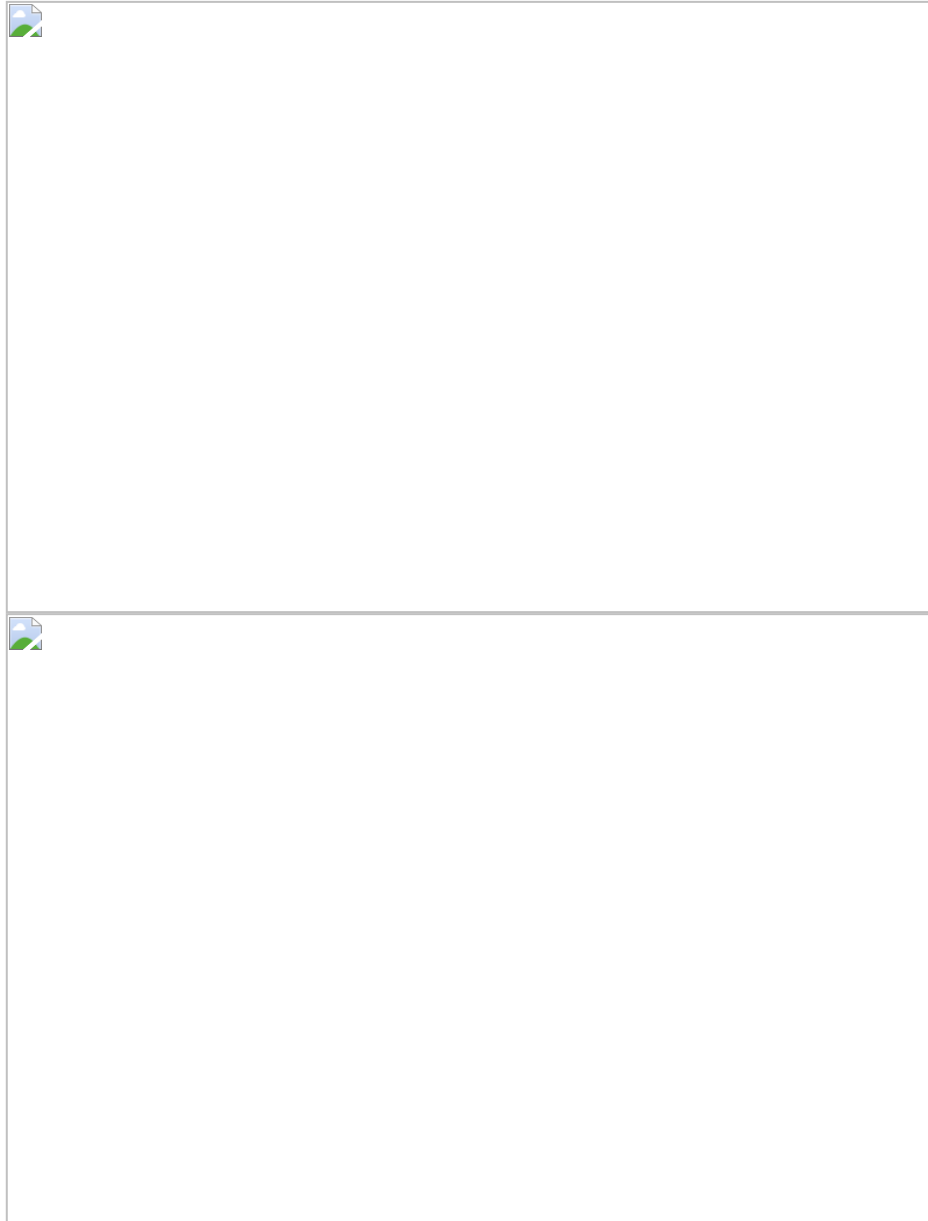




Figure 17. Magnetic sensitivity of QHS 6.144-MHz AT-cut resonators made with different spring materials. (a) Kovar, (b) nickel, (c) stainless steel, (d) stainless steel (other kind), and (e) copper alloy.

V. ORIGIN OF THE MAGNETIC SENSITIVITY OF QUARTZ RESONATORS

Several effects could exist at the origin of the magnetic sensitivity of the quartz resonator. Nevertheless, many of them have such a weak influence that they cannot explain the observed sensitivity. For example, it is known that quartz is diamagnetic. Its magnetic susceptibility has been measured to be $X_m = -0.46 \cdot 10^{-6}$ [15]. When exposed to an inhomogeneous magnetic field, a diamagnetic material of volume τ experiences a force given by



directed in the decreasing magnetic field sense [16]. Assuming a linearly decreasing field 20 G (2 mT) with a maximum gradient of 0.15 mT/m, the resulting force would be 10^{-14} N. The stress induced by this force in the quartz plate and the resulting frequency change is not simple to calculate. Nevertheless, taking the worst-case estimate of a diametrical compression [17], the relative frequency shift induced by such a weak force would be in the 10^{-18} range.

Another magnetic effect concerns the change in the resonator motional resistance due to the eddy currents produced in the electrodes by their motion in the external magnetic field. An assessment of the frequency deviation due to this effect in a 20-G (2-mT) magnetic field for an AT-cut with 1-mm Cu electrodes gives an effect in the 10^{-22} range [13].

Magnetostriction of the electrodes when they are made of ferromagnetic material has also been considered but, once again, the order of magnitude is in the 10^{-14} range for a 5-MHz AT-cut in a 20-G (2-mT) magnetic field [2].

In addition, magnetic sensitivity is observed even when the electrodes are made of nonferromagnetic material so that other magnetomechanical effects, such as the Delta- E effect of the electrodes, cannot explain the frequency deviation [3].

The only remaining source of magnetomechanical action is the ferromagnetic nature of the springs used to hold the quartz plate. The various mechanisms that can be considered to explain how a magnetic field induces a mechanical action in a ferromagnetic material will be briefly presented here [18].

A. Compass Effect

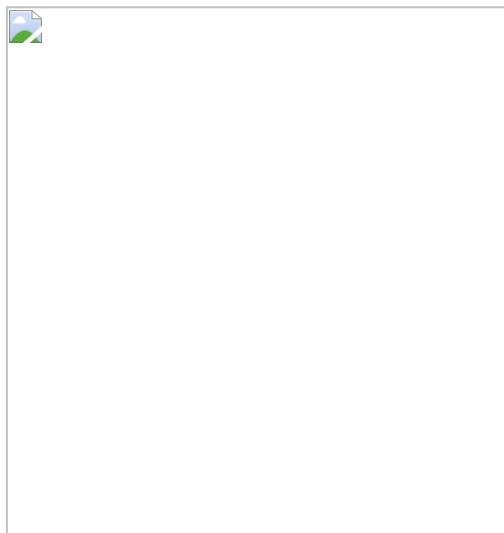


Figure 18. Compass effect.

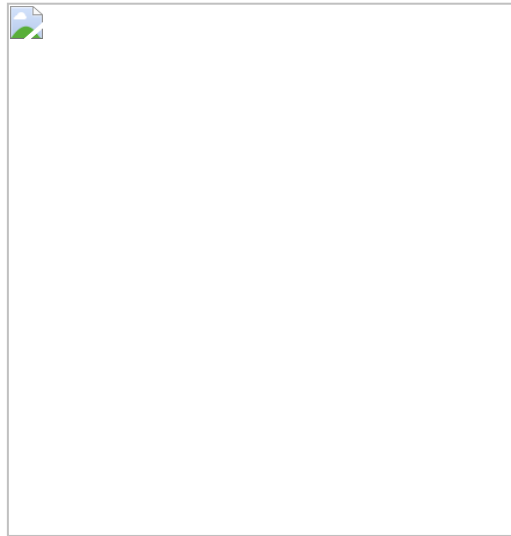


Figure 19. Bending of the assembly.

The first effect is explained by the fact that ferromagnetic materials are constituted of small magnetic domains initially randomly oriented. When submitted to a magnetic field, these domains tend to align along the direction corresponding to the easiest magnetization direction, which is usually the rolling direction of the material. As the domains reach the saturation state, their magnetization vectors oriented along the same direction are subject to a torque tending to align them with the external magnetic field, just like a compass needle. This situation is sketched in Fig. 18.

Since the supports of the quartz plate are clamped on the base, the assembly could bend as shown in Fig. 19, resulting in a maximum effect when the magnetic field lies in the plane of the supports.

It should be noted that a change in the magnetic field sense also changes the sense of the magnetization vector so that the resulting torque does not change.

B. Mutual Repulsion

Two parallel ferromagnetic supports close together submitted to a magnetic field act as two small magnets of same polarity. As a consequence, they tend to repel each other and to induce a diametrical tension in the quartz plate they support (see Fig. 20).

As in the previous case, a change in the applied magnetic field sense also changes both magnet polarities so that the resulting effect is always a mutual repulsion.

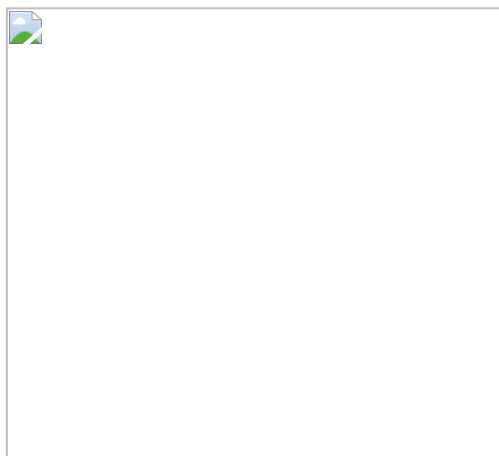
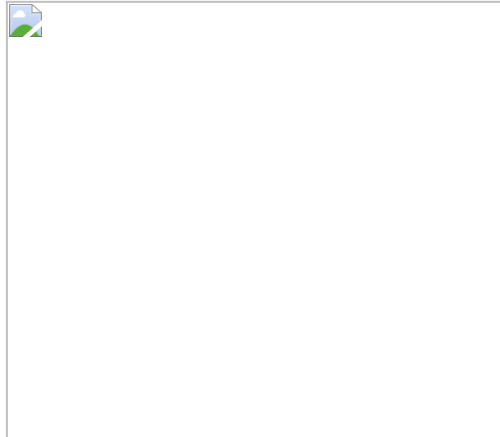
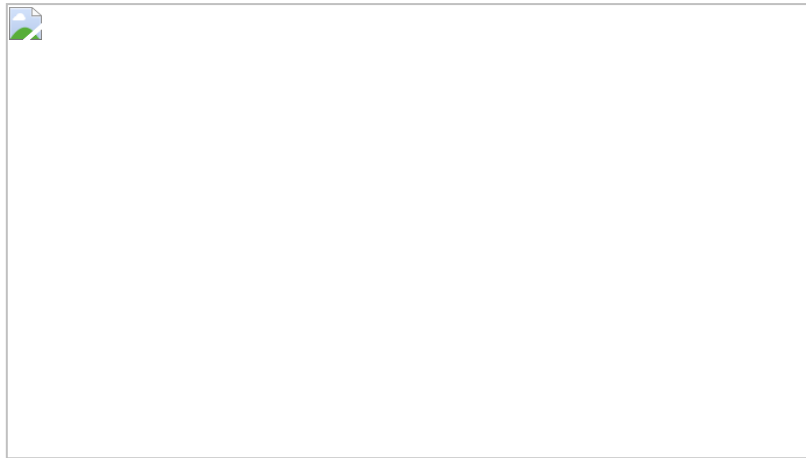


Figure 20. Repulsion forces.

C. Change of Elastic Modulus

This effect, also called *Delta-E effect*, consists of a change in the Young's modulus of ferromagnetic materials when submitted to a magnetic field. As a result, the pressure exerted by a ferromagnetic spring on a sustained disc is modified by an external magnetic field (see Fig. 21). Fig. 22 shows the variation of Young's modulus for various ferromagnetic material [\[18\]](#). The sign of this variation does not depend on the sense of the magnetic field.

Figure21. Delta-*E* effect.Figure 22. Change in Young's modulus with magnetization (after [\[18\]](#)).

D. Magnetostriction

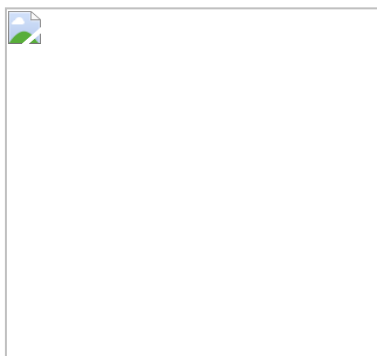


Figure 23. Magnetostriction.

The last magneto-mechanic effect is the magnetostriction, which is a change in the dimensions of a ferromagnetic material submitted to a magnetic field. For example, as shown in Fig. 23, a rod of nickel submitted to a magnetic field undergoes a contraction in length and an expansion in the other directions so that the volume is kept approximately constant. In many cases, ferromagnetic materials may present an expansion in length rather than a contraction. In all cases, the deformation (contraction or expansion) only depends on the kind of material, but not on the sense of the applied magnetic field. Fig. 24 shows the magnetostriction coefficient of some ferromagnetic materials [18].

The kovar used in various parts of the resonator packaging (see Fig. 1) is also a ferromagnetic material, the magnetostriction of which has been measured at the *Laboratoire de Magnétisme Louis Neel* in Grenoble. The result is shown in Fig. 25 [19].

It is easy to understand that the magnetostriction of the springs and/or the supports can induce stress in the disc they sustain.

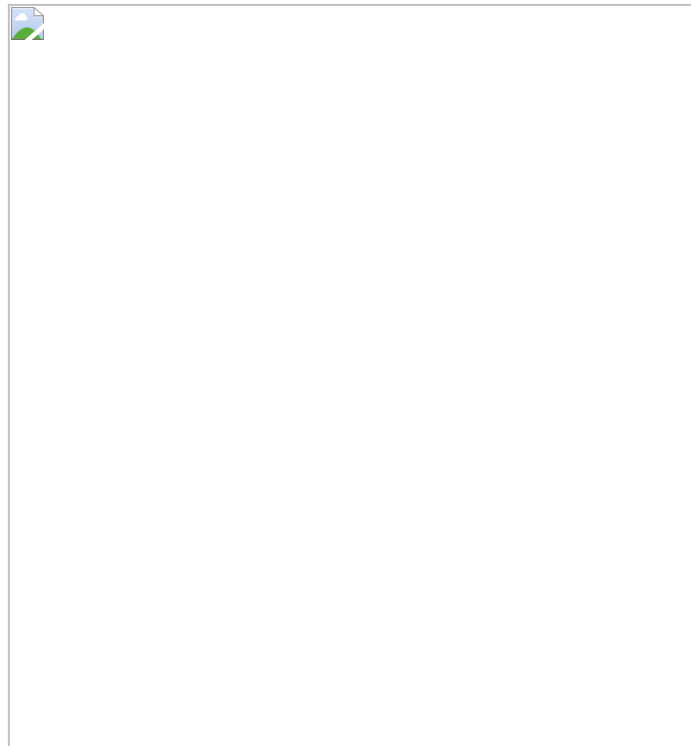


Figure 24. Magnetostriction of some ferromagnetic materials (after [18]).

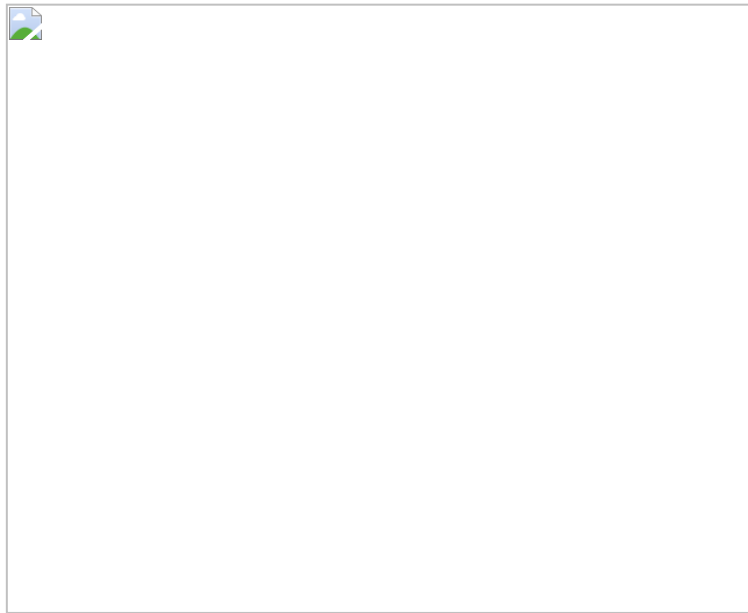


Figure 25. Magnetostriction of Kovar (after [\[19\]](#)).

E. Hysteresis

Most of the magnetic effects described above do not depend on the sense of the applied magnetic field and present a maximal effect when the field is directed along the largest dimension of the material. Also, most of these magnetic effects present a more or less pronounced hysteresis depending on the kind of material. For example, Fig. 26 shows the hysteresis of magnetostriction in nickel [\[18\]](#). It is interesting to note the similarity between the magnetostriction hysteresis curve (Fig. 26) and the resonator magnetic sensitivity shown in Fig. 14, for example.

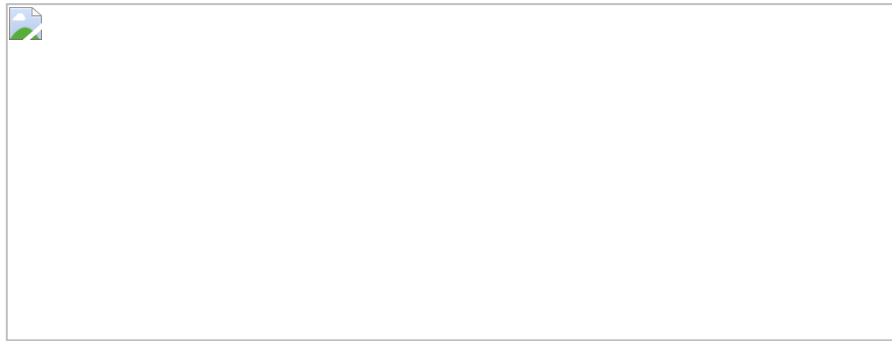


Figure 26. Hysteresis of the magnetostriction in nickel (after [\[18\]](#)). (a) Well-annealed and (b) hard and partially annealed.

F. Discussion

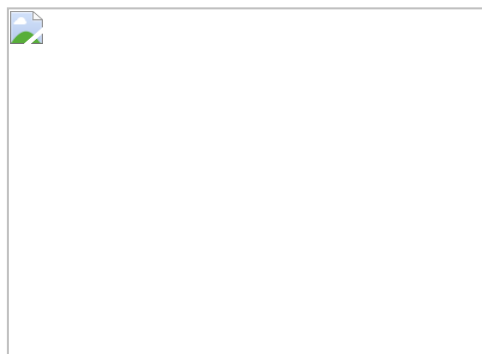


Figure 27. Most sensitive direction of the magnetic effect.

In almost all magnetic sensitivity measurements performed on resonators, the maximal effect is observed when the magnetic field is directed normal to the plane of the resonator plate [4] (see Fig. 27). This fact implies that the "compass effect" is probably not responsible for the observed sensitivity.

The order of magnitude of the repulsion forces between the two supports is not consistent with the stresses necessary to account for the observed resonator magnetic sensitivity, thus this effect should be also discarded.

For some time, the magnetostriction was considered as the most probable magnetoelastic effect responsible for the resonator magnetic sensitivity because of the similarity between the magnetic sensitivity curve of the resonator (Fig. 14) and the magnetostriction hysteresis curve of the spring material [20] (Fig. 26). Nevertheless, with regard to the geometry of the plate mounting (Fig. 1) only the lateral magnetostrictive expansion of the spring may induce stresses in the plate and the order of magnitude of this expansion (a few nm) is hardly consistent with the observed frequency variation. Thus the magnetostriction is probably not the most important cause of the resonator magnetic sensitivity.

The only remaining effect is the Young's modulus change. In fact, when the quartz disc is mounted, it is gripped by the two nickel springs so that the plate is prestressed by the supports, any change in the Young's modulus of the springs will modify the diametrical forces acting on the plate and then its resonant frequency. The curve plotted in Fig. 22 shows that, the Young's modulus of nickel may increase from about 6% up to 16% when the material reaches its saturation state (a few tens of gauss). This order of magnitude is fully consistent with the observed frequency changes.

VI. CONCLUSION

The magnetic sensitivity of resonators comes undoubtedly from the ferromagnetic properties of the springs used to hold the quartz plate. This sensitivity can be drastically reduced by using copper alloy springs. Kovar and nickel should be avoided. Although the quartz plate itself is not responsible for the magnetic sensitivity, the magnitude of the phenomenon can be strongly increased by the geometrical characteristics of the disc; it is obvious that the thicker the plate the lower the sensitivity. Even in a same lot of resonators, a great variety of magnetic signatures is often observed, some of them being abnormally asymmetrical in view of the magnetic action and geometric assembly symmetries. It is highly probable that these anomalies betray a geometric asymmetry in the plate mounting. In most of the experiments, the higher sensitivity is observed when the magnetic field is directed along the resonator axis that is along the largest dimension of the springs.

Among the possible magnetoelastic effects responsible for the resonator magnetic sensitivity, the most important is probably the change in the Young's modulus of the spring material although, in some cases, the magnetostriction should not be entirely discarded.

It is highly probable that the complexity of the magnetic signature has to be attributed to the spring Young's modulus hysteresis rather than to a complicated stress and strain interaction between plate and springs. This interaction might be as simple as a diametrical tension or compression for which the induced frequency shift is well characterized. Then, the magnetic sensitivity of resonators could constitute an extremely sensitive tool for the experimental investigations on the mechanical actions exerted on the resonator plate. In fact, by knowing the magnetic behavior of the spring, it is possible to determine the kind of the actions the plate is submitted to and the device thus obtained can be easily used, for example, to experimentally determine the lowest sensitivity fastening points on the plate or to study new shapes of springs and supports.

These applications still need theoretical modeling of the magneto-elastic behavior of the various materials and it is in these directions that efforts are currently continuing.

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